

tps

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Newton & Gravity

◆ Objectives

- Why do the planets go around the Sun/Moons go around planets?
- Newton's laws of motion
- Newton's law of gravity
- Earth-Moon tides

Isaac Newton

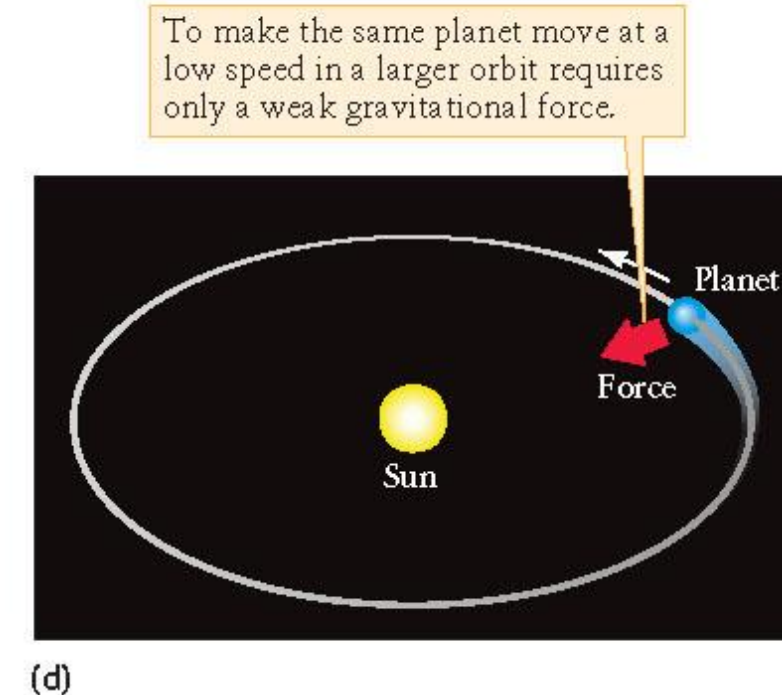
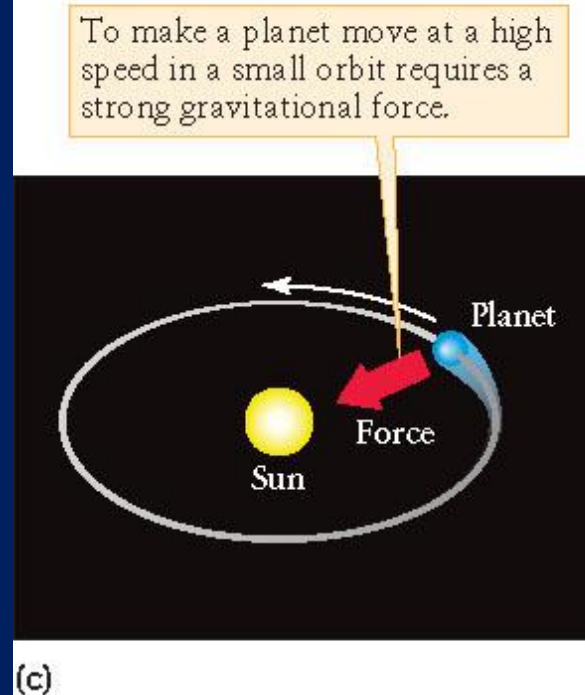
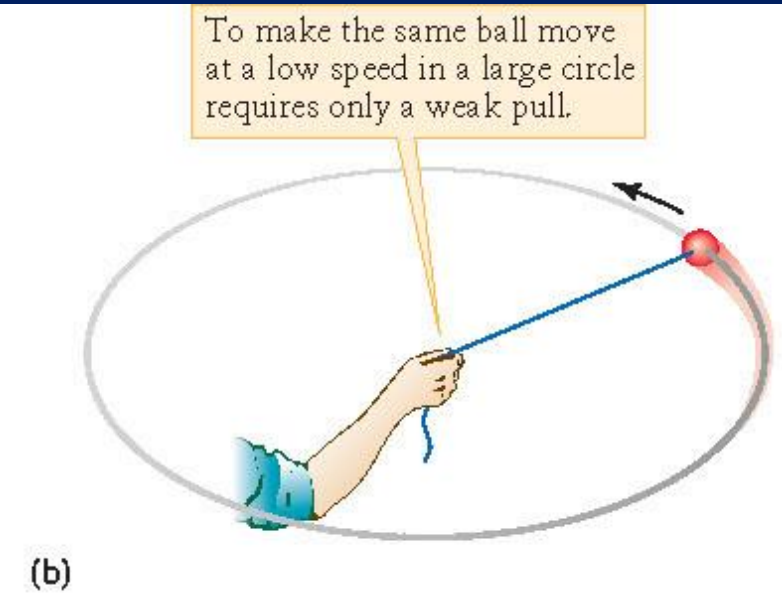
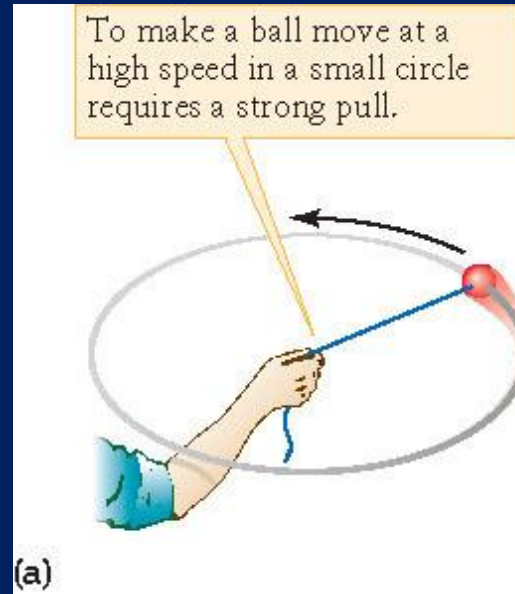
- Kepler and others' work took observations and built models to fit those observations
- Newton developed Laws of Motion (3 of them) that apply to all objects, and then showed that **Kepler's laws were a direct consequence of these laws.**
- These laws are truly universal- **they don't just apply to planets and orbital motion, but motion here on Earth or anywhere else in the universe.**

1st Law: Inertia

- ◆ An object that is at rest will remain at rest; and an object in motion will remain in motion, ***unless acted on by a net outside force.***
- ◆ Why Don't the Planets Fly Off Into Space???

Demo

- ◆ Why Don't the Planets Fly Off Into Space???
- ◆ A Force is acting on the planets
- ◆ This is what Newton deduced



2nd Law

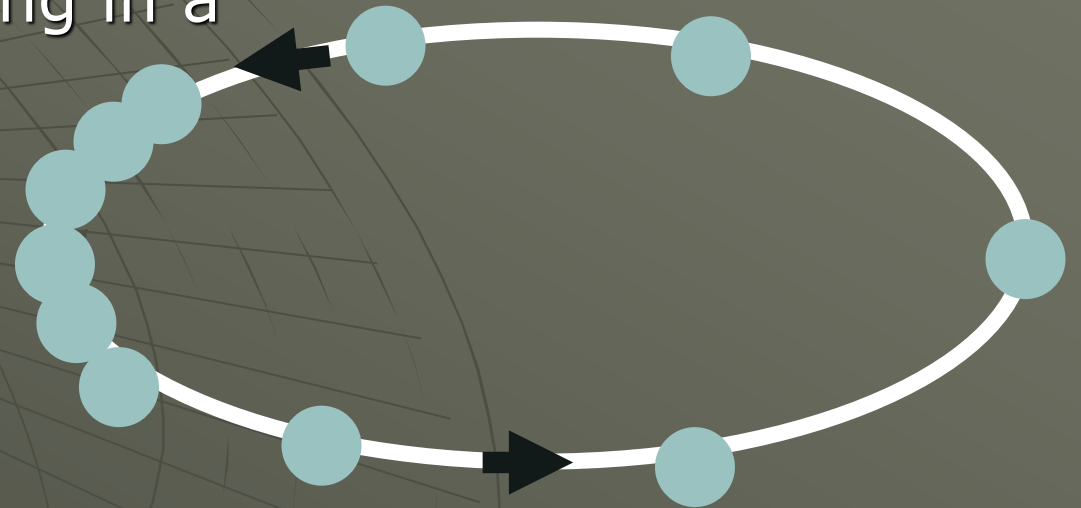
- ◆ The (net) force acting on an object is equal to object's mass times its acceleration.

$$\mathbf{F = ma}$$

- ◆ ***a=acceleration (units m/s^2): change in an object's speed or direction***
 - On *Earth* $a=9.8\ m/s^2$
- ◆ ***m=Mass (units kg):*** is a measure of an object's **inertia**.
- ◆ **F=Force (units Newton)**
- ◆ **Weight:** Measure of force acting on a mass
- ◆ As force on object goes up, acceleration increases
- ◆ The more massive an object, the more difficult to accelerate object

Be careful...

- ◆ Object speeding up **or** slowing down is *accelerating*.
- ◆ Object moving at constant speed, but **changing direction** is *accelerating*.
 - Example: planet in an elliptical or circular orbit
 - Force **required** to keep planet moving in a circle
 - Remember: ball on a string demo



Units

- ◆ What is the unit of a Newton???
- ◆ $a = \text{m/s}^2$
- ◆ $m = \text{kg}$
- ◆ $F = ma$; units = $\text{kg} * \text{m/s}^2$
- ◆ $N = \text{kg} * \text{m/s}^2$

Unit Analysis

Q: A 200 kg car changes it's speed by 10 m/s in 10 seconds. How many Newtons of force acted on the car?

- A. 20 N
- B. 100 N
- C. 200 N
- D. 2000 N

$$A: N = \text{kg} \cdot \text{m/s}^2$$

$$200 \text{ (kg)} * 10 \text{ (m/s)} / 10 \text{ (s)} = 200 * 1 = 200 \text{ N}$$

tps

Q: A person has a mass of 50 kg. What is their weight on Earth?

A) 490 N (or 110 lbs)

B) 300 N (or 67 lbs)

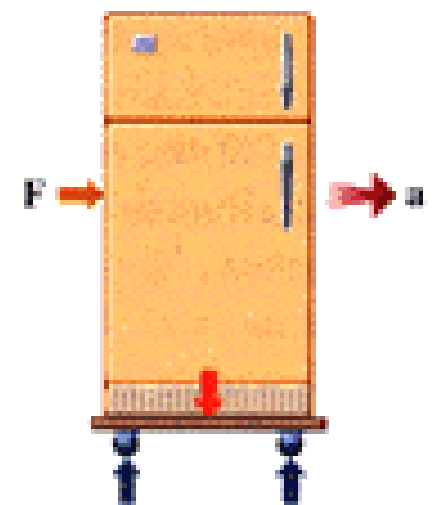
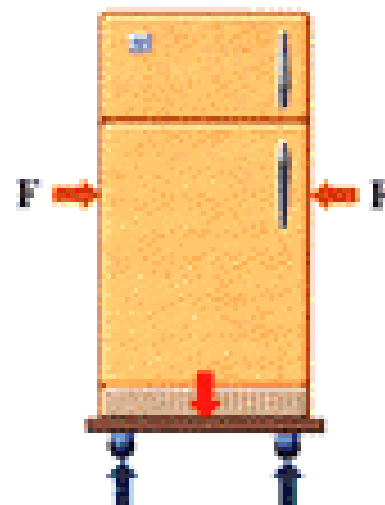
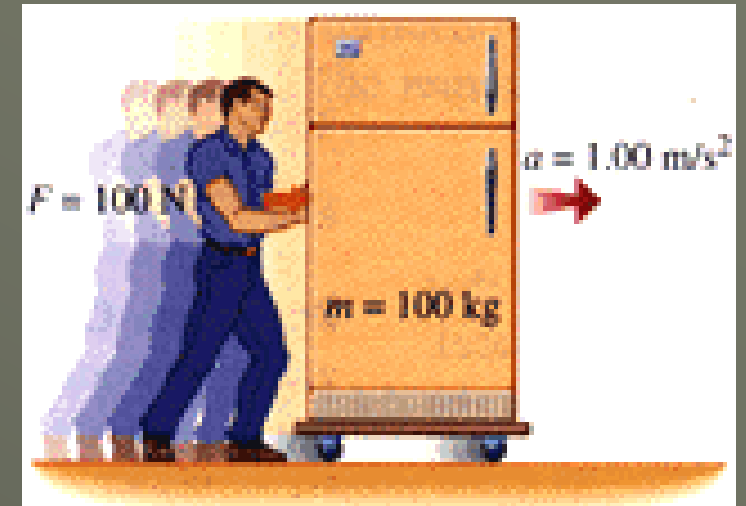
C) 50 kg (or 50 lbs)

D) 8000 N (or 1,797 lbs)



Net Force

- Net = Summation of all forces (add up all forces)



Q: Which of the following cars does NOT experience an acceleration?

- A. A car driving due north at a speed of 60 mph
- B. A car coming to a stop at a red light
- C. A car driving around a curve at a constant speed of 30 mph
- D. A car entering a highway and matching its speed to the faster-moving cars

Q: In which of the following cases is a net outside force acting upon an object?

- A. A box sits at rest on the floor.
- B. A car drives due north at a speed of 60 miles per hour.
- C. A hockey puck glides across the ice.
- D. A block of wood, after being pushed across a table, eventually stops.

Newton's Third Law of Motion

- Whenever one object exerts a force on a second object, the second object exerts an equal and opposite force on the first object (action-reaction)
- Earth pulls on moon with the same force that moon pulls on earth!
- You are exerting a gravitational force on me, the building, your book, etc!

Example: If you weight 120 lbs, when you sit in a chair you exert a force of 120 lbs on the chair. The chair reacts and pushes against you with a force of 120 lbs.

- Hint: Are you moving? Why aren't you falling?

Newton's Laws & Heliocentricity

- With this simple formalism, Newton's laws explain **WHY** the heliocentric model is true
- 3rd law says that if the Sun exerts a force on the planets, the planets exert the same force on the Sun
- The 2nd law says that since the Sun is much more massive than the planets, the same force yields a much smaller acceleration for the Sun
- Thus, it is the planets that move (accelerate) and orbit!

Newton's Law of Gravitation

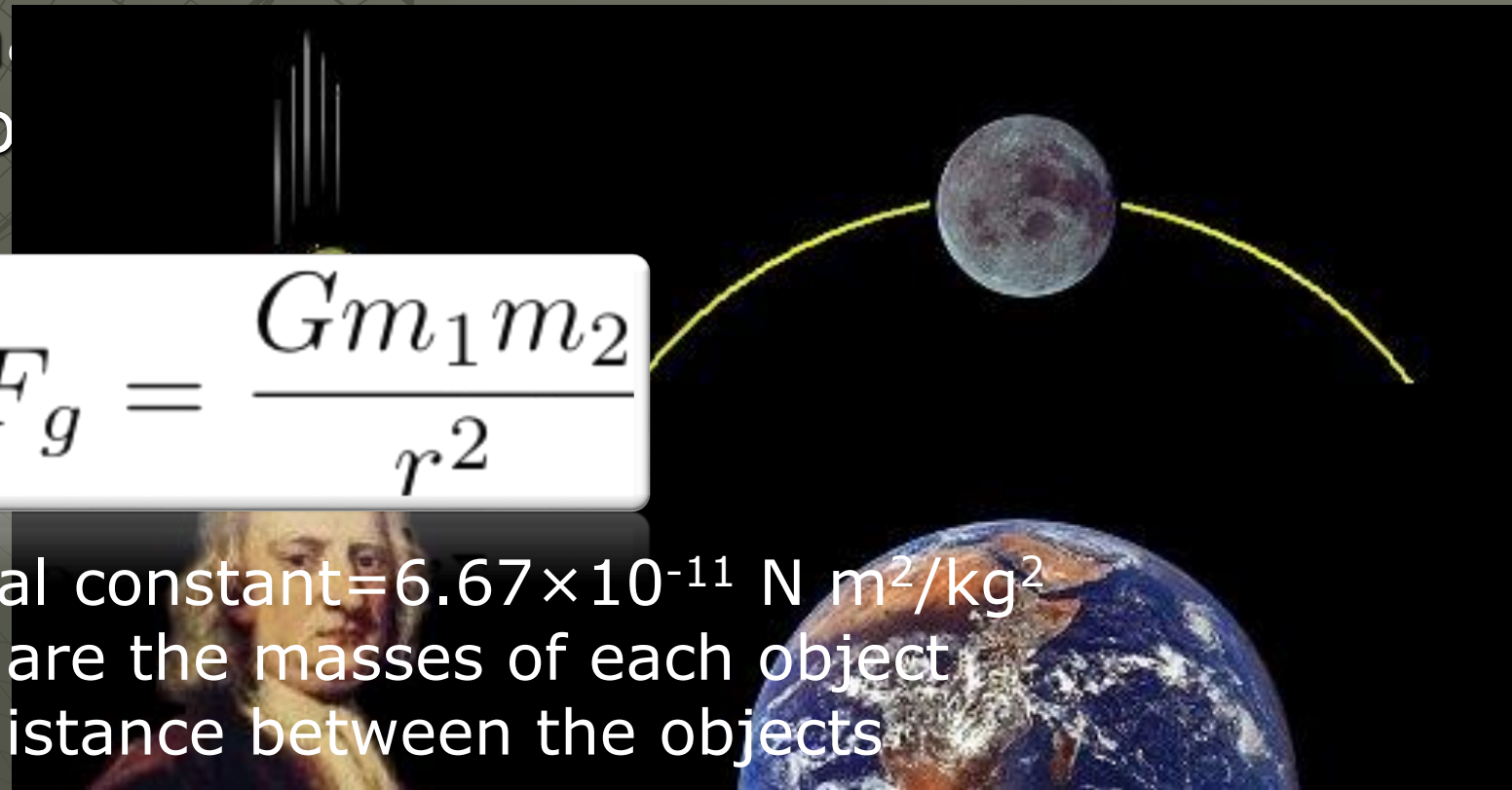
- ◆ Newton's First law shows that the planets are acted upon by a force which Newton called gravity
- ◆ Same force that "pulls" an apple from a tree
- ◆ Two objects attract each other with a force that is directly proportional to the product of their masses and inversely proportional to the square of the distance between them

$$F_g = \frac{Gm_1m_2}{r^2}$$

G=gravitational constant= $6.67 \times 10^{-11} \text{ N m}^2/\text{kg}^2$

m_1 and m_2 are the masses of each object

r is the distance between the objects



Why does a feather and a rock hit the ground together?

- ◆ Objects fall according to Newton's 2nd law:
 - $F=ma$
- ◆ Gravity is the force responsible for falling:
 - $F=GMm/r^2$ (M=mass of Earth, m=mass of object)

$$\frac{GMm}{r^2} = ma$$
$$a = \frac{GM}{r^2}$$

- a is independent of mass of the object!!!

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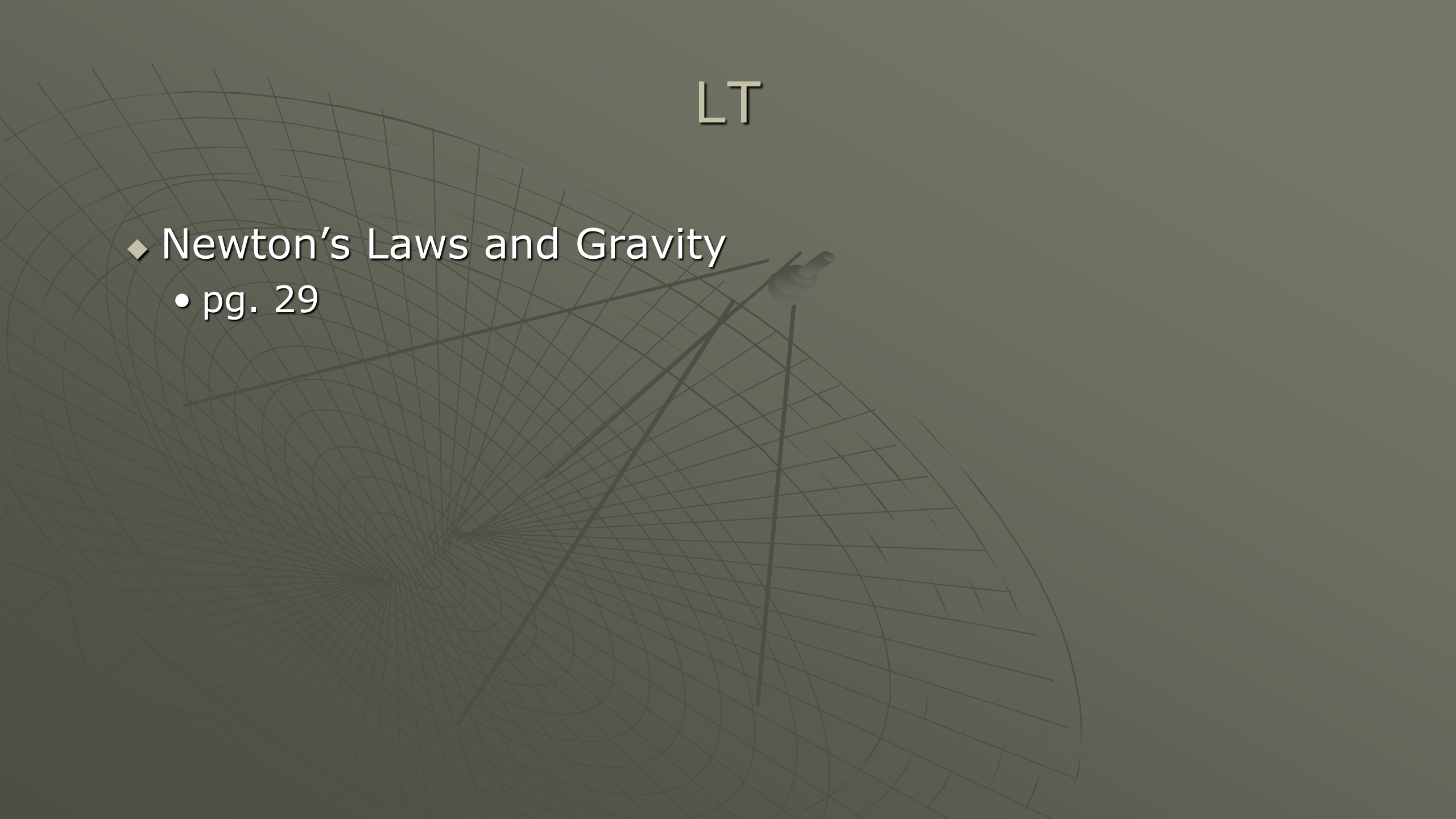
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Q: On which of the following objects would a person have the least mass?

- A. Earth
- B. Jupiter
- C. The Moon
- D. A person's mass would be the same on all three.

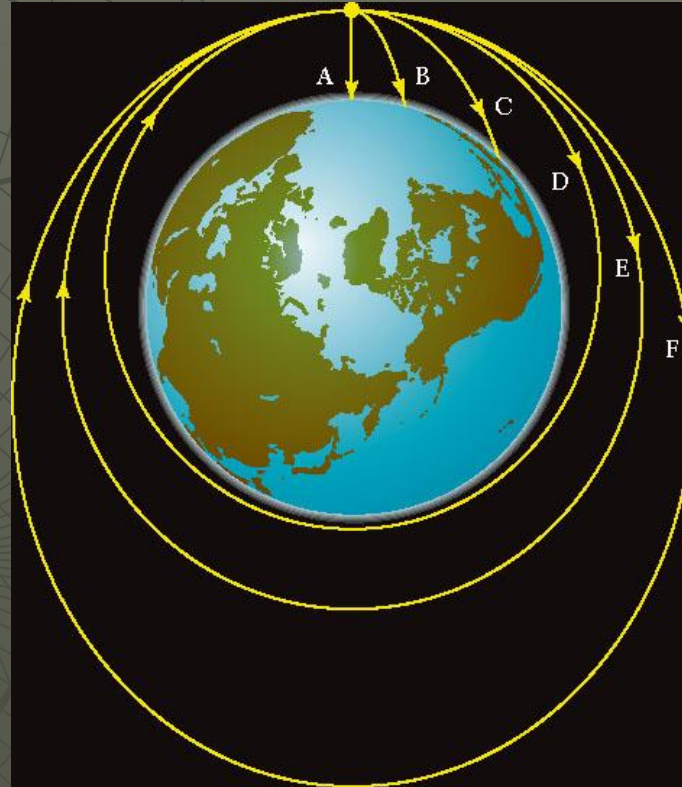
LT

- ◆ Newton's Laws and Gravity
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Gravity and Orbits

- So if all objects attract each other, why don't the planets just all fall into the sun?



[Animation](#)

Orbiting objects are always falling; they're just falling *around* the Earth! (or whatever they're orbiting)

Gravity and Orbits

- Newton also generalized Kepler's third law ($P^2=a^3$) to any bodies in orbit around each other (Kepler's law only applies to things orbiting the Sun)

$$P^2 = \left(\frac{4\pi^2}{G(m_1 + m_2)} \right) a^3$$

- $M (\text{sun}) = 2 \times 10^{30} \text{ kg!!!}$
- $M (\text{earth}) = 6 \times 10^{24} \text{ kg}$
- $m_1 + m_2 = 2.000006 \times 10^{30} \text{ kg}$

Newtonian Mechanics

- Can mathematically explain and predict all the orbits of the planets, satellites, and most things in the universe
- Was used to predict the existence of Neptune, before it was ever seen
- Still used in many situations today, but not all...Einstein

Tidally Locked

- Same face no matter what phase!!!
- The far side of the Moon was not seen in its entirety until 1959, when photographs were transmitted from the Soviet spacecraft Luna 3.
- Does the moon rotate???



new moon



new crescent



first quarter



waxing gibbous



full moon



waning gibbous



last quarter

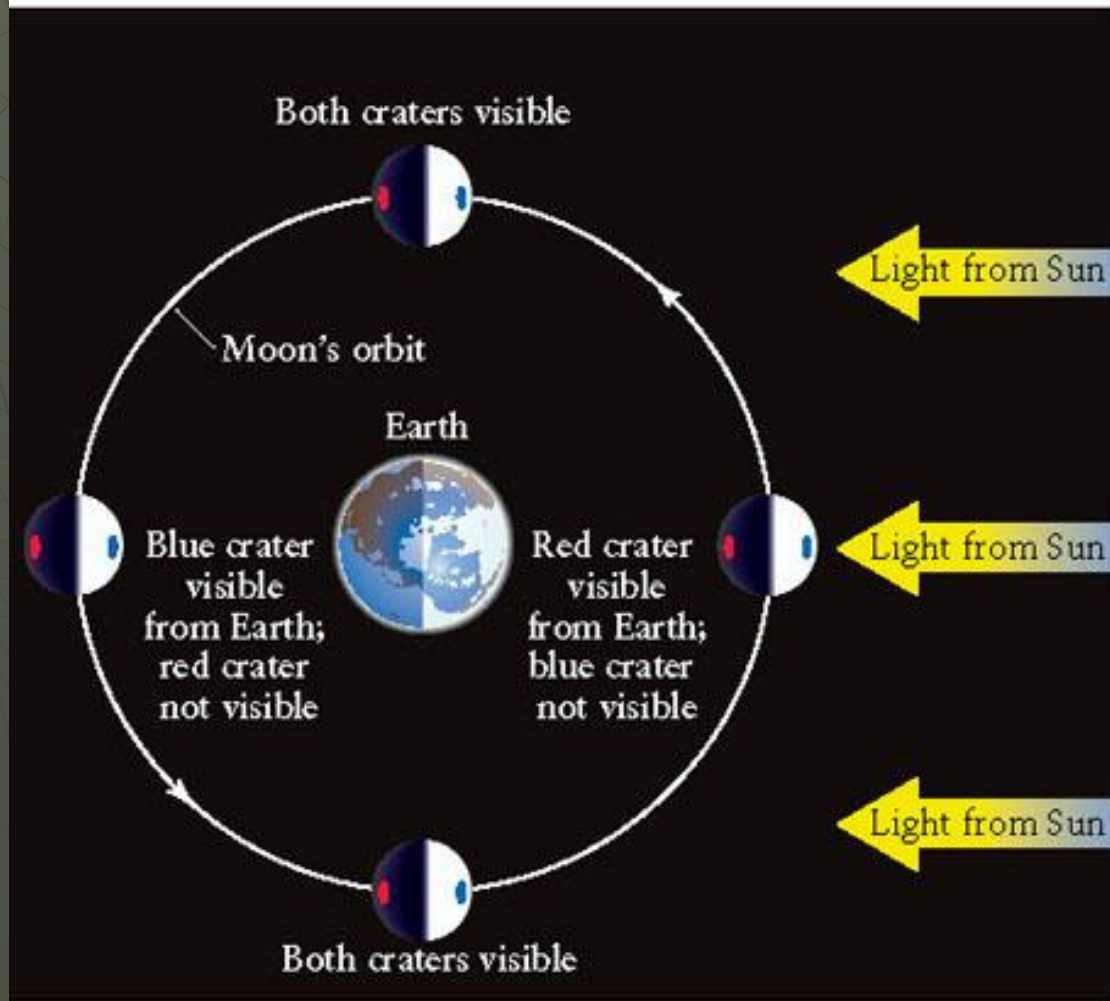


old crescent

www.visualdictionaryonline.com

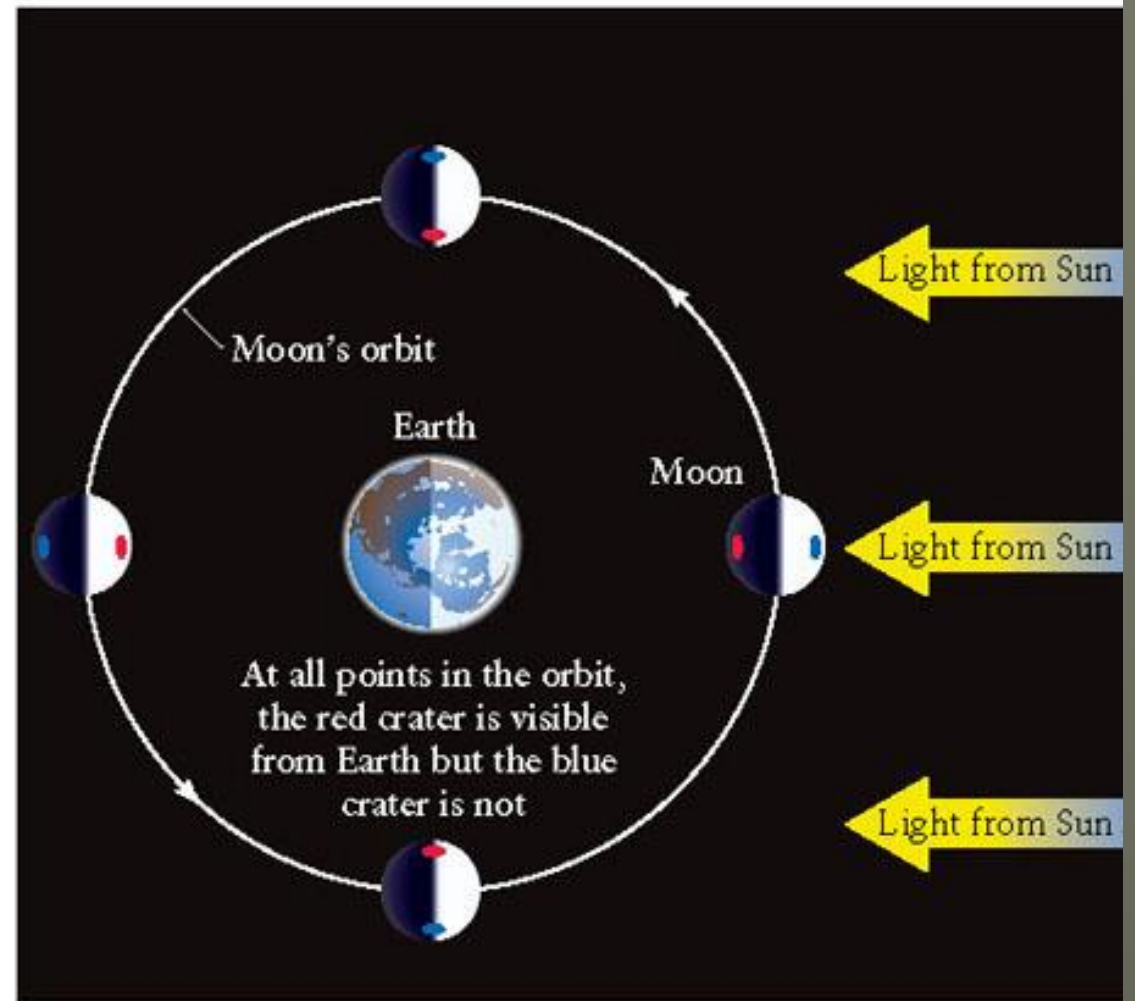
Moon's Rotation???

If the Moon did not rotate,
we could see all sides of the Moon



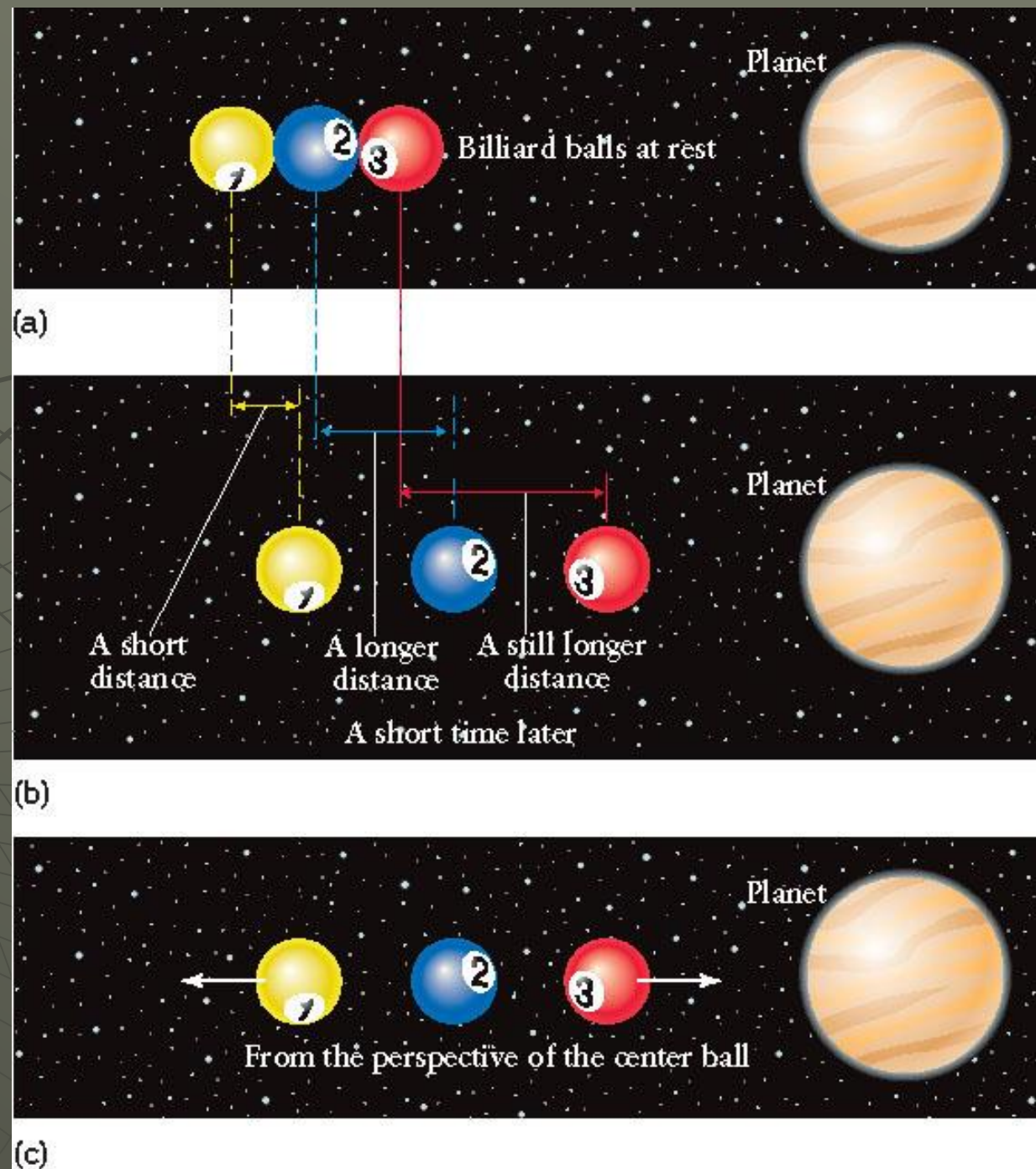
(a)

In fact, the Moon does rotate,
and we see only one face of the Moon



(b)

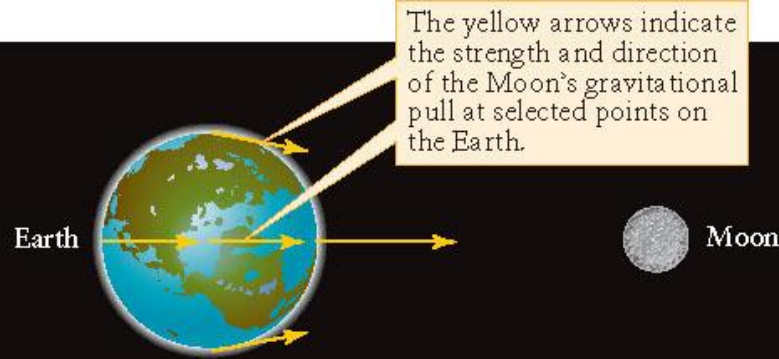
Tidal Forces???



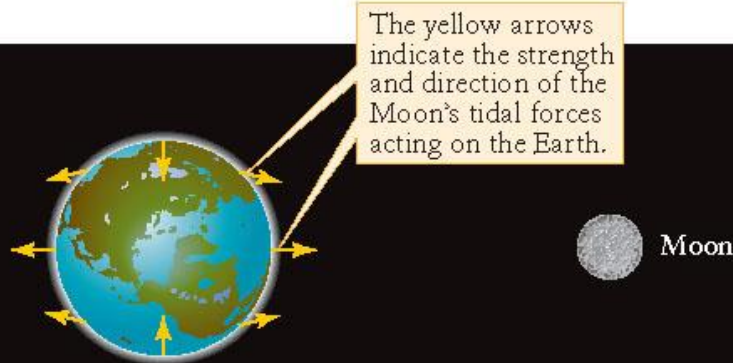
Tides

- Pull from the Moon and Sun cause the water on Earth to bulge

Mostly Due to the Moon



(a)



From the perspective of the center of the Earth

(b)

As the Earth rotates underneath the oceans, a given location experiences alternating high tides and low tides.

This person is at low tide

This person is at high tide

Moon

Earth

Oceans

This person is at high tide

This person is at low tide

(a)

The greatest deformation (spring tides) occurs when the Sun, Moon, and Earth are aligned and the tidal effects of the Sun and Moon reinforce each other.

Moon

Sun

Spring tide

(b)

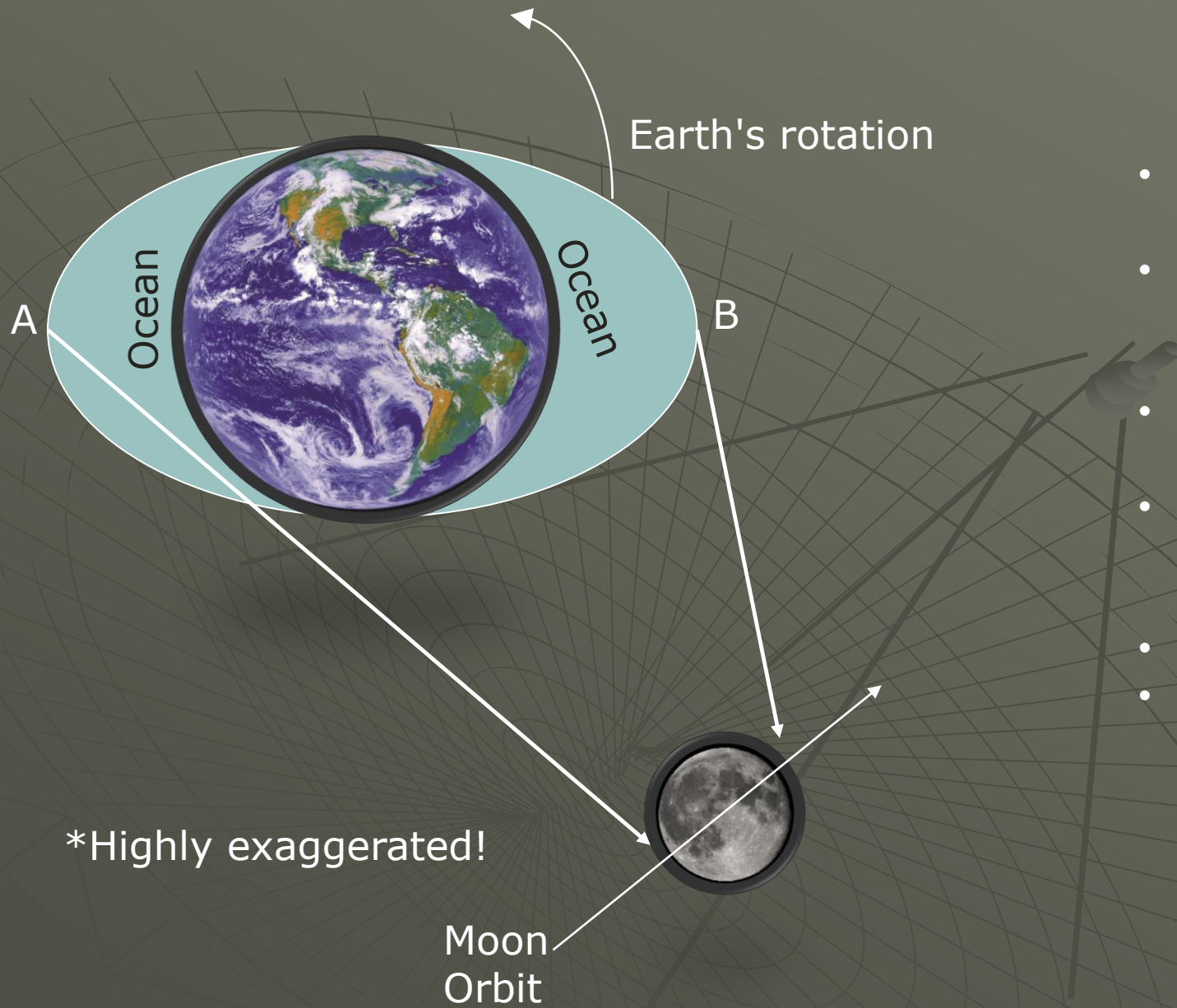
The least deformation (neap tides) occurs when the Sun, Earth, and Moon form a right angle and the tidal effects of the Sun and Moon partially cancel each other.

Moon

Sun

Neap tide

(c)



*Highly exaggerated!

- The Moon causes bulges in the Earth's oceans
- The Earth rotates faster than the moon's orbit (gets ahead of the moon)
- Point B pulls on leading edge of the moon
- Point A pulls on the trailing edge of the moon
- Angular momentum
- The Moon is slowly moving away from us by $\sim 3\text{cm/year!!!}$

- ◆ A consequence of the moon-earth tidally locked system, the moon:
 - A. Doesn't rotate
 - B. Rotates at the same rate as it orbits the earth
 - C. Rotates once a day
 - D. Rotates so fast, that cheese bits fly off of its surface!